Year 1 - 6

Calculation Policy

Multiplication and Division

#MathsEveryoneCan



Notes and Guidance

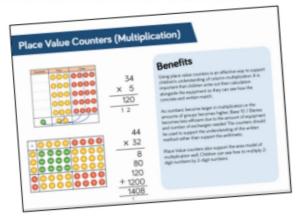
White Rose Maths

Calculation Policy

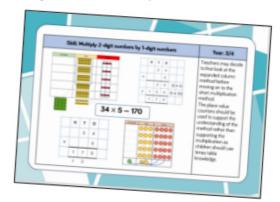
Welcome to the White Rose Maths Calculation Policy.

This document is broken down into addition and subtraction, and multiplication and division.

At the start of each policy, there is an overview of the different models and images that can support the teaching of different concepts. These provide explanations of the benefits of using the models and show the links between different operations.

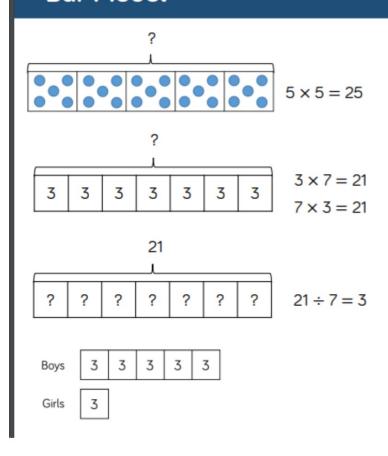


Each operation is then broken down into skills and each skill has a dedicated page showing the different models and images that could be used to effectively teach that concept.



There is an overview of skills linked to year groups to support consistency through out school. A glossary of terms is provided at the end of the calculation policy to support understanding of the key language used to teach the four operations.

Bar Model



Benefits

Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.

Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups.

It is important when solving word problems that the bar model represents the problem.

Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there?

The multiple bar model provides an opportunity to compare the groups.

Number Shapes



$$5 \times 4 = 20$$

 $4 \times 5 = 20$



$$5 \times 4 = 20$$

 $4 \times 5 = 20$



$$18 \div 3 = 6$$



Benefits

Number shapes support children's understanding of multiplication as repeated addition.

Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g. odd \times odd = even, odd \times even = odd, even \times even = even.

When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how many groups of the number there are altogether e.g. There are 6 groups of 3 in 18.

Bead Strings



$$5 \times 3 = 15$$

 $3 \times 5 = 15$

$$15 \div 3 = 5$$



$$5 \times 3 = 15$$

 $3 \times 5 = 15$

$$15 \div 5 = 3$$



$$4 \times 5 = 20$$

 $5 \times 4 = 20$

$$20 \div 4 = 5$$

Benefits

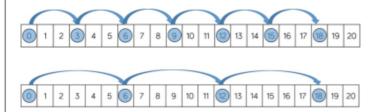
Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.

Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.

Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.

When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 – Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.

Number Tracks



$$6 \times 3 = 18$$

 $3 \times 6 = 18$



 $18 \div 3 = 6$

Benefits

Number tracks are useful to support children to count in multiples, forwards and backwards. Moving counters or cubes along the number track can support children to keep track of their counting. Translucent counters help children to see the number they have landed on whilst counting.

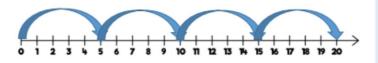
When multiplying, children place their counter on 0 to start and then count on to find the product of the numbers.

When dividing, children place their counter on the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0. Children record how many jumps they have made to find the answer to the division.

Number tracks can be useful with smaller multiples but when reaching larger numbers they can become less efficient.

Number Lines (labelled)





$$4 \times 5 = 20$$

 $5 \times 4 = 20$



 $20 \div 4 = 5$

Benefits

Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.

When multiplying, children start at 0 and then count on to find the product of the numbers.

When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0.

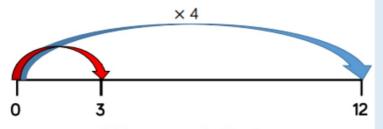
Children record how many jumps they have made to find the answer to the division.

Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.

Number Lines (blank)



A red car travels 3 miles. A blue car 4 times further. How far does the blue car travel?



A blue car travels 12 miles.
A red car 4 times less.
How far does the red car travel?

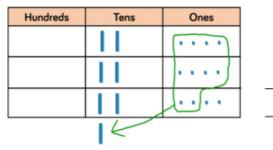
Benefits

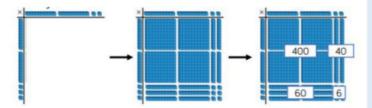
Children can use blank number lines to represent scaling as multiplication or division.

Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.

Blank number lines without intervals can also be used for children to represent scaling.

Base 10/Dienes (multiplication)





Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.

Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2-digits.

Base 10/Dienes (division)



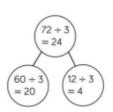


$$68 \div 2 = 34$$



| Tens | Ones | | |
|------|---------|--|--|
| | • | | |
| | • • • • | | |
| | • • • • | | |

$$72 \div 3 = 24$$



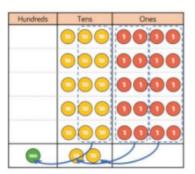
Benefits

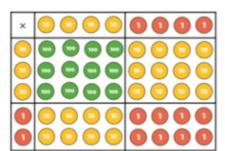
Using Base 10 or Dienes is an effective way to support children's understanding of division.

When numbers become larger, it can be an effective way to move children from representing numbers as ones towards representing them as tens and ones in order to divide. Children can then share the Base 10/ Dienes between different groups e.g. by drawing circles or by rows on a place value grid.

When they are sharing, children start with the larger place value and work from left to right. If there are any left in a column, they exchange e.g. one ten for ten ones. When recording, encourage children to use the partwhole model so they can consider how the number has been partitioned in order to divide. This will support them with mental methods.

Place Value Counters (multiplication)





| × | 44 32 |
|------|----------|
| | 8 |
| | 80 |
| | 120 |
| + 12 | 200 |
| 14 | 108 |
| 1 | |

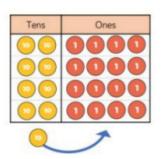
Benefits

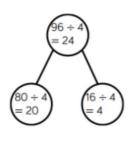
Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.

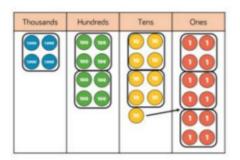
As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed The counters should be used to support the understanding of the written method rather than support the arithmetic.

Place value counters also support the area model of multiplication well. Children can see how to multiply 2-digit numbers by 2-digit numbers.

Place Value Counters (division)







1223 4 489¹2

Benefits

Using place value counters is an effective way to support children's understanding of division.

When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.

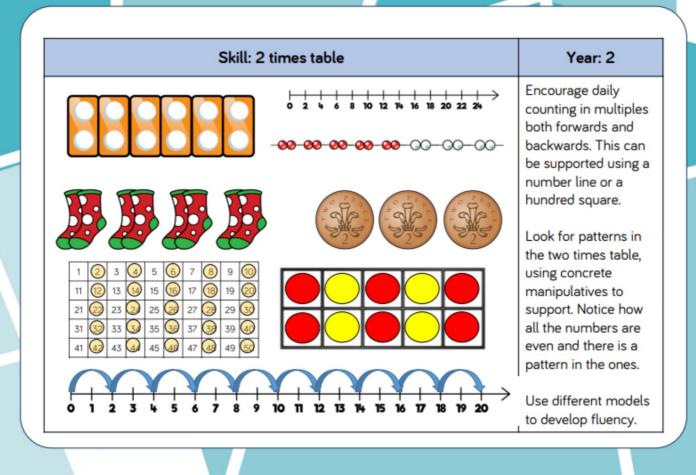
Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.

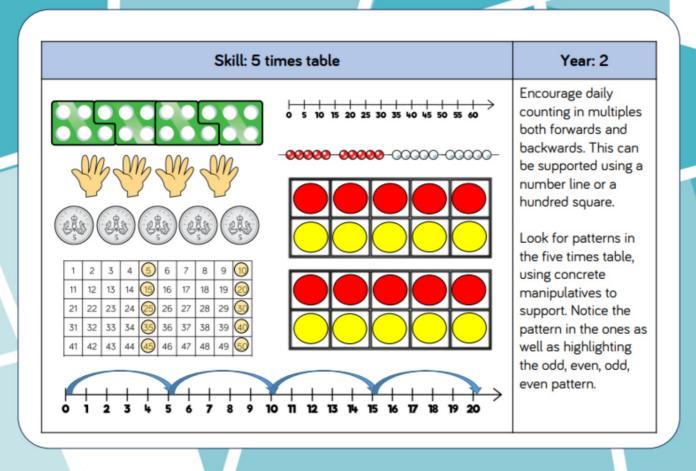
Times Tables

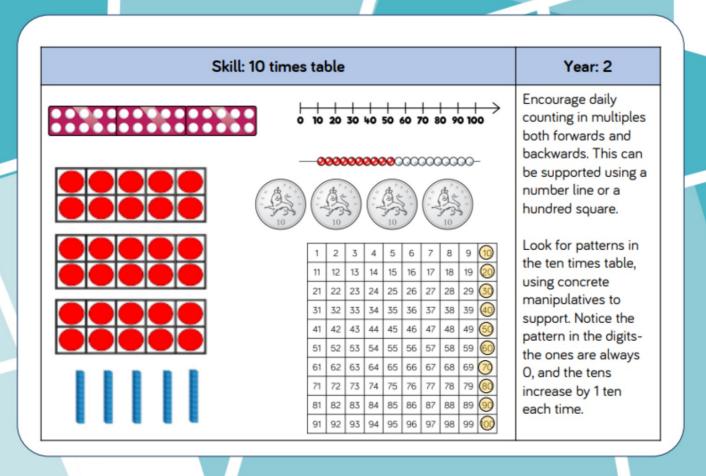
| Skill | Year | Representations and models | |
|------------------------|------|----------------------------|------------------|
| Recall and use | 2 | Bar model | Ten frames |
| multiplication and | | Number shapes | Bead strings |
| division facts for the | | Counters | Number lines |
| 2-times table | | Money | Everyday objects |
| Recall and use | 2 | Bar model | Ten frames |
| multiplication and | | Number shapes | Bead strings |
| division facts for the | | Counters | Number lines |
| 5-times table | | Money | Everyday objects |
| Recall and use | 2 | Hundred square | Ten frames |
| multiplication and | | Number shapes | Bead strings |
| division facts for the | | Counters | Number lines |
| 10-times table | | Money | Base 10 |

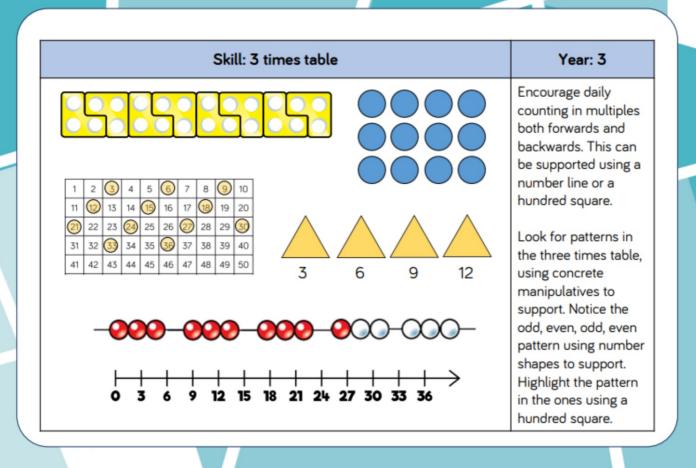
| Skill | Year | Representations and models | |
|---|------|---|---|
| Recall and use multiplication and division facts for the 3-times table | 3 | Hundred square Number shapes Counters | Bead strings Number lines Everyday objects |
| Recall and use multiplication and division facts for the 4-times table | 3 | Hundred square Number shapes Counters | Bead strings Number lines Everyday objects |
| Recall and use multiplication and division facts for the 8-times table | 3 | Hundred square Number shapes | Bead strings Number tracks Everyday objects |
| Recall and use multiplication and division facts for the 6-times table | 4 | Hundred square Number shapes | Bead strings Number tracks Everyday objects |

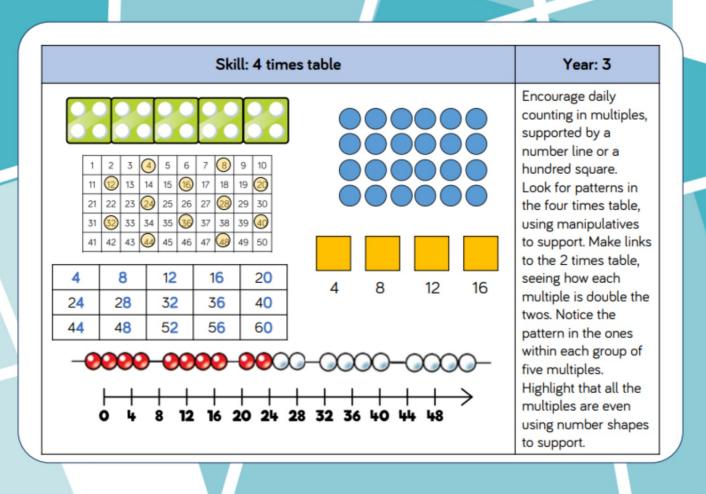
| Skill | Year | Representations and models | |
|--|------|---------------------------------|--------------------------------------|
| Recall and use multiplication and division facts for the 7-times table | 4 | Hundred square Number shapes | Bead strings Number lines |
| Recall and use multiplication and division facts for the 9-times table | 4 | Hundred square Number shapes | Bead strings Number lines |
| Recall and use multiplication and division facts for the 11-times table | 4 | Hundred square Base 10 | Place value counters Number lines |
| Recall and use multiplication and division facts for the 12-times table | 4 | Hundred square Base 10 | Place value counters Number lines |

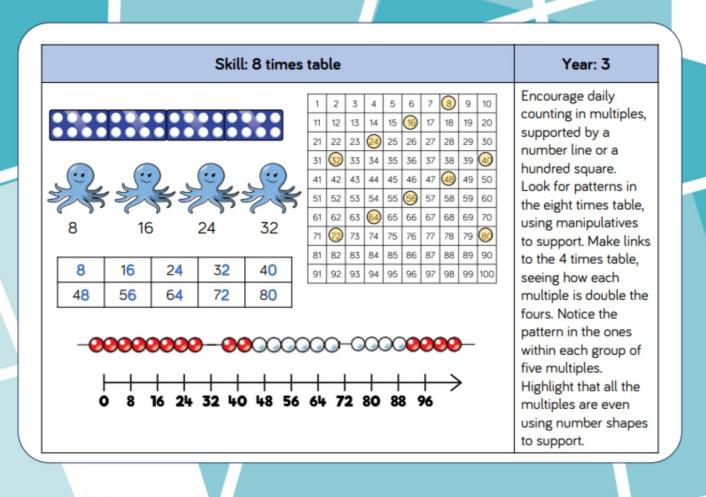


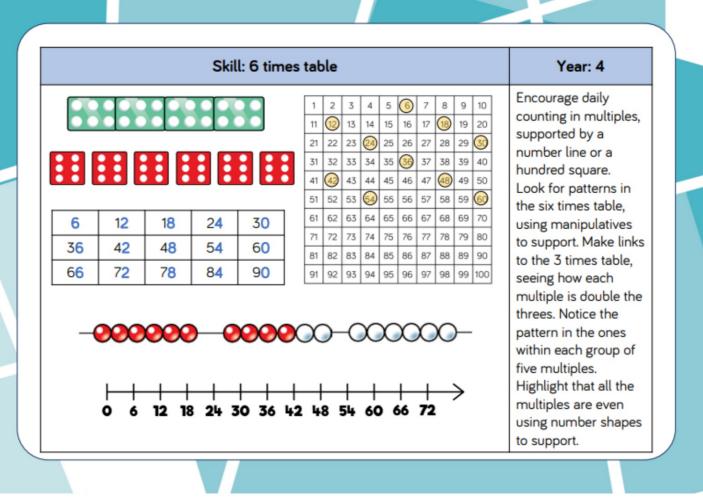


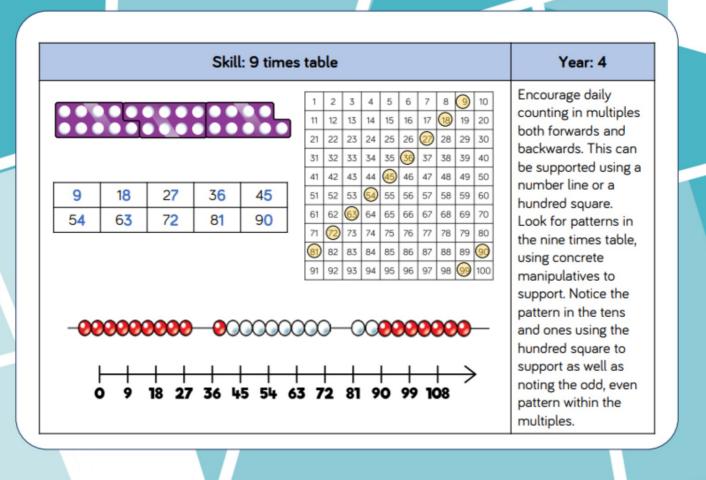


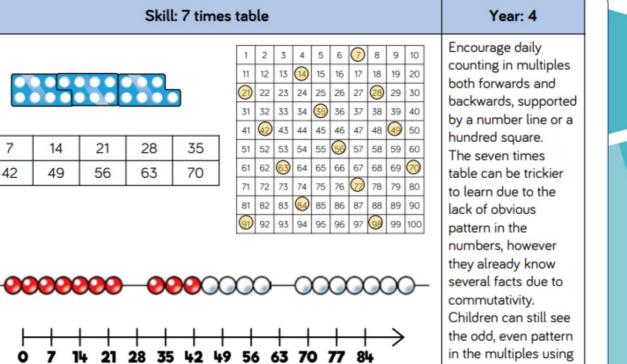






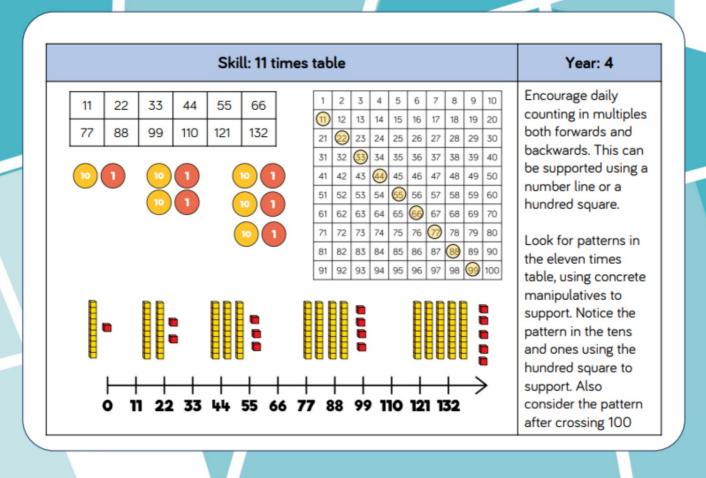


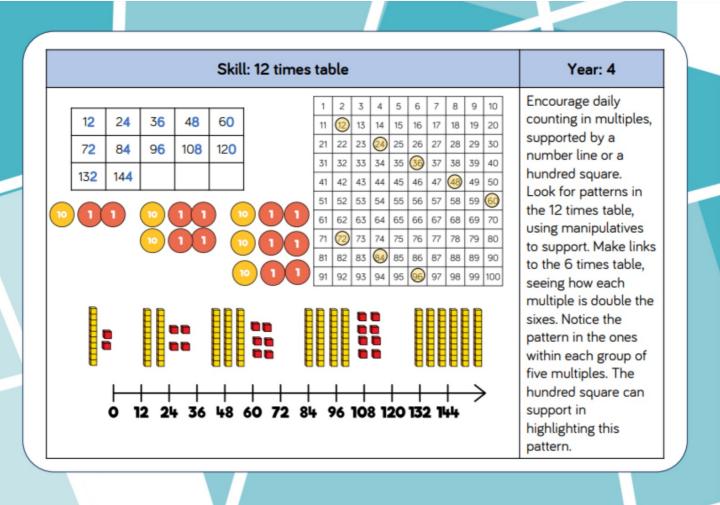




number shapes to

support.

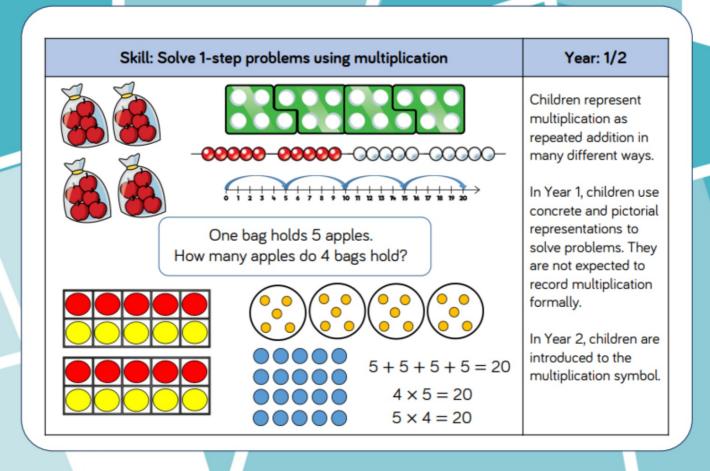


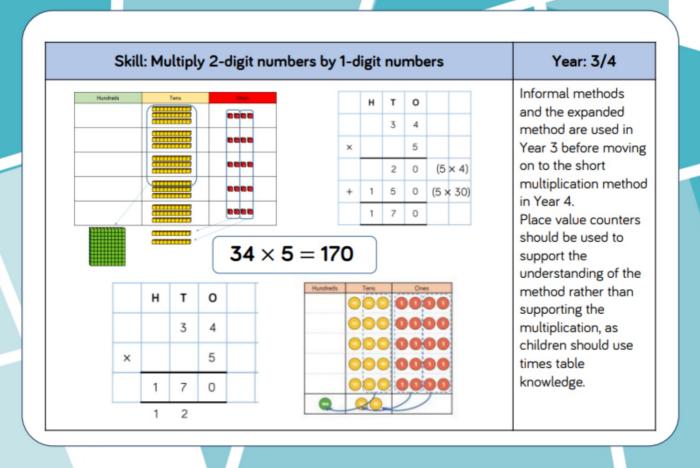


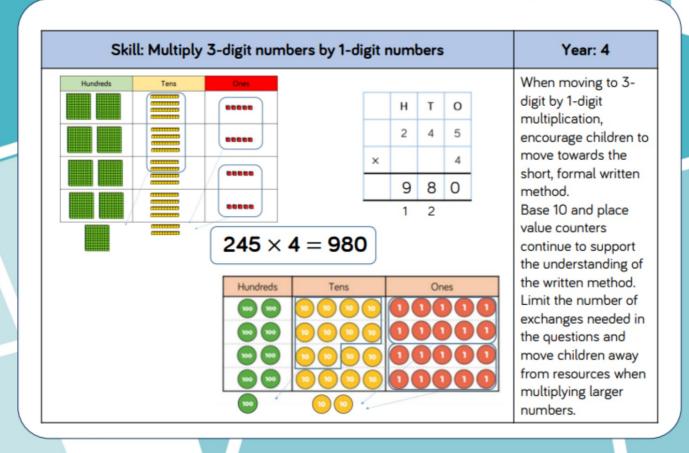
Multiplication

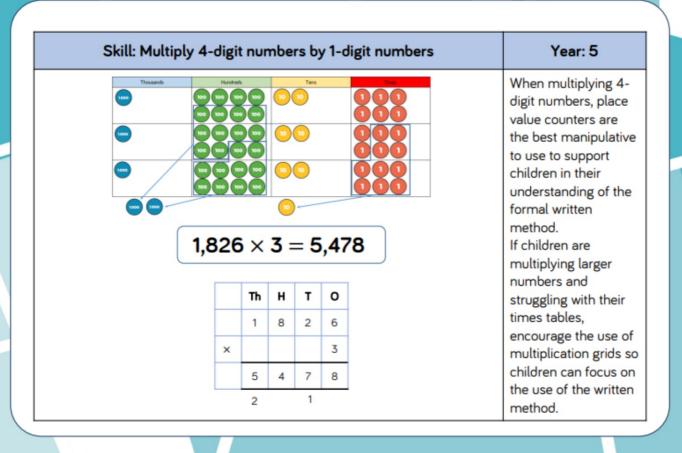
| Skill | Year | Representations and models | |
|---|------|--|---|
| Solve one-step problems with multiplication | 1/2 | Bar model Number shapes Counters | Ten frames Bead strings Number lines |
| Multiply 2-digit by 1- digit numbers | 3/4 | Place value counters Base 10 | Expanded written method Short written method |
| Multiply 3-digit by 1- digit numbers | 4 | Place value counters Base 10 | Short written method |
| Multiply 4-digit by 1- digit numbers | 5 | Place value counters | Short written method |

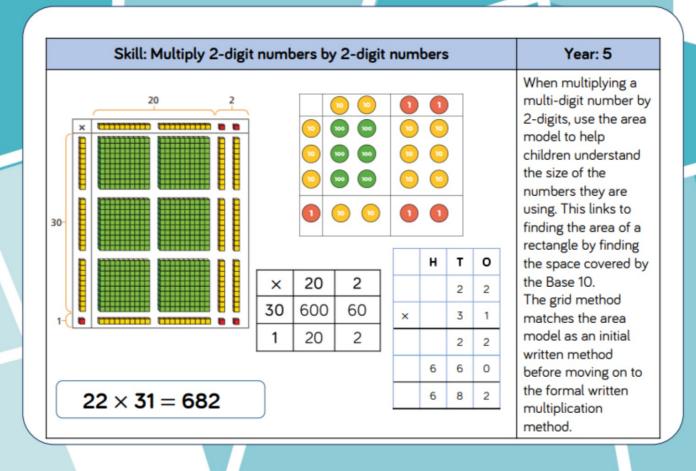
| Skill | Year | Representations and models | |
|---|------|---------------------------------|--|
| Multiply 2-digit by 2- digit numbers | 5 | Place value counters Base 10 | Short written method Grid method Formal written method |
| Multiply 2-digit by 3- digit numbers | 5 | Place value counters | Short written method Grid method Formal written method |
| Multiply 2-digit by 4- digit numbers | 5/6 | Formal written method | |











Skill: Multiply 3-digit numbers by 2-digit numbers

| Th | н | т | 0 |
|-----|----|---|---|
| | 2 | 3 | 4 |
| × | | 3 | 2 |
| | 4 | 6 | 8 |
| 1 7 | 10 | 2 | 0 |
| 7 | 4 | 8 | 8 |

| × | 200 | 30 | 4 |
|----|-------|-----|-----|
| 30 | 6,000 | 900 | 120 |
| 2 | 400 | 60 | 8 |

Year: 5

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.

Children should now move towards the formal written method, seeing the links with the grid method.

 $234 \times 32 = 7,488$

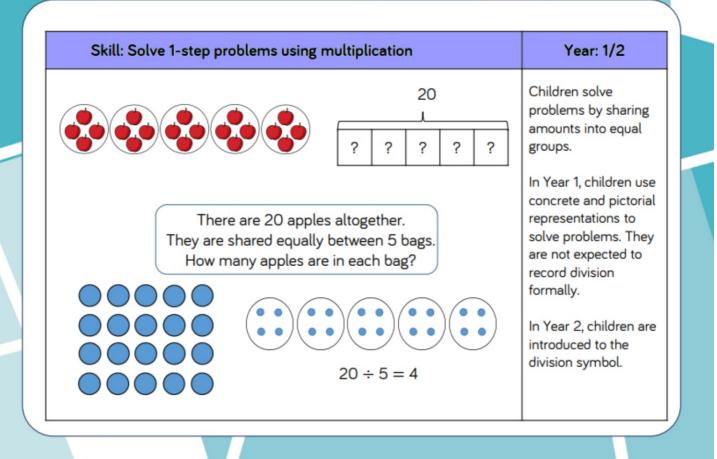
| Skill: Multiply 4-digit numbers by 2-digit numbers | | | | | | | Year: 5/6 |
|--|--------|--------|---|--------|---|--|--|
| | TTh | Th | н | Т | 0 | | When multiplying 4- digits by 2-digits, children should be |
| | | 2 | 7 | 3 | 9 | | confident in using the formal written method. |
| | × | | | 2 | 8 | | If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method. |
| | 2 | 1 5 | 9 | 1 7 | 2 | | |
| | 5 1 | 4 | 7 | 8 | 0 | | |
| | 7 | 6 | 6 | 9 | 2 | | |
| 2,739 × 28 = 76,692 | | | | | | Consider where exchanged digits are placed and make sure this is consistent. | |

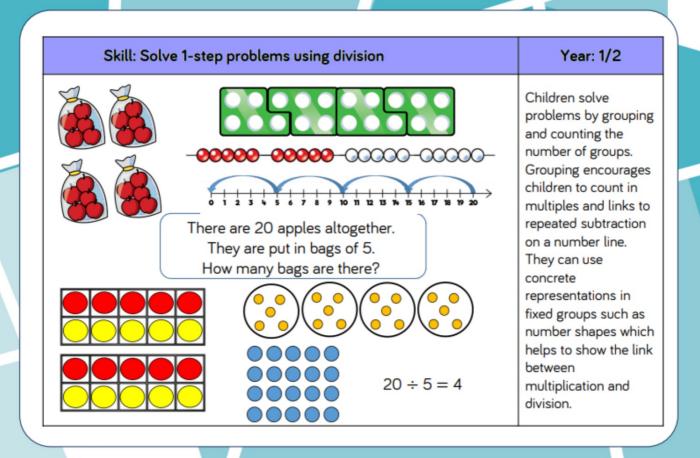
Division

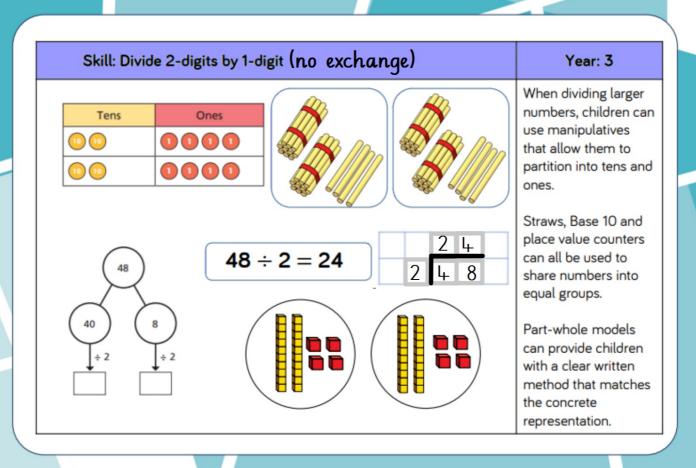
| Skill | Year | Representations and models | | |
|--|------|--|--|--|
| Solve one-step problems with division | 1/2 | Bar model Real life objects | Arrays Counters | |
| Solve one-step problems with division | 1/2 | Real life objects Number shapes Bead strings Ten frames | Number lines Arrays Counters | |
| Divide 2-digits by 1-digit (no exchange) | 3 | Straws Base 10 Bar model | Place value counters Part-whole model Written short division | |
| Divide 2-digits by 1-digit (exchange) | 3 | Straws Base 10 Bar model | Place value counters Part-whole model Written short division | |

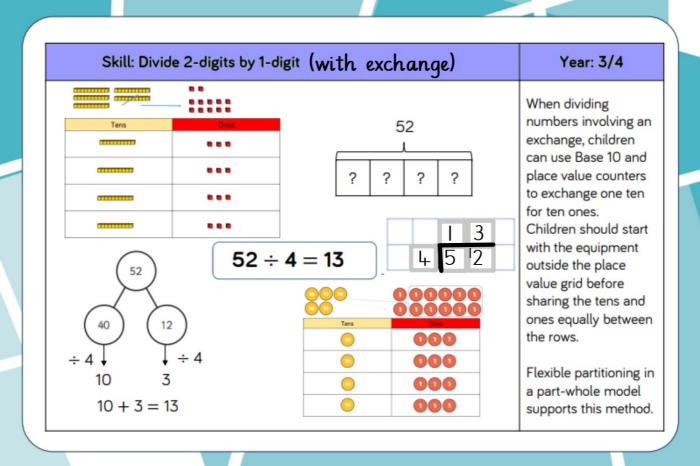
| Skill | Year | Representations and models | | | |
|---|------|----------------------------------|--|--|--|
| Divide 2-digits by 1-digit (remainders) | 3/4 | Straws Base 10 Bar model | Place value counters Part-whole model Written short division | | |
| Divide 2-digits by 1- digit | 4/5 | Place value counters Counters | Place value grid Written short division | | |
| Divide 3-digits by 1- digit (exchange) | 4 | Base 10 Bar model | Place value counters Part-whole model Written short division | | |
| Divide 3-digits by 1- digit | 4/5 | Place value counters Counters | Place value grid Written short division | | |

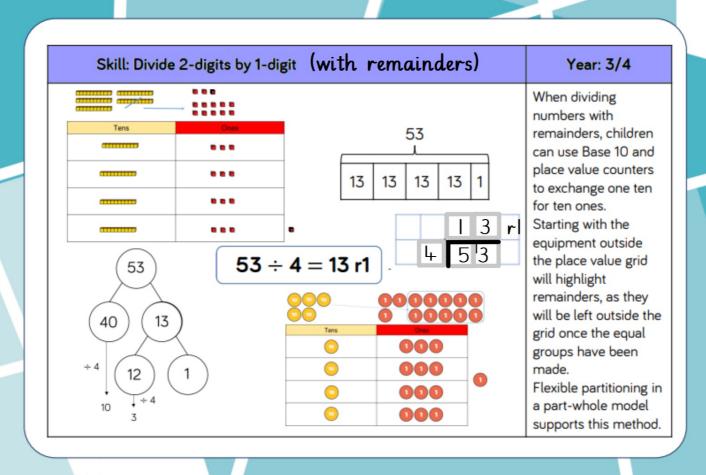
| Skill | Year | Representations and models | | | |
|--|------|----------------------------------|---|--|--|
| Divide 4-digits by 1- digit | 5 | Place value counters Counters | Place value grid Written short division | | |
| Divide multi-digits by 2-digits (short division) | 6 | Written short division List | List of multiples of partitioned multiples | | |
| Divide multi-digits by 2-digits (long division) | 6 | Written long division | List of multiples | | |

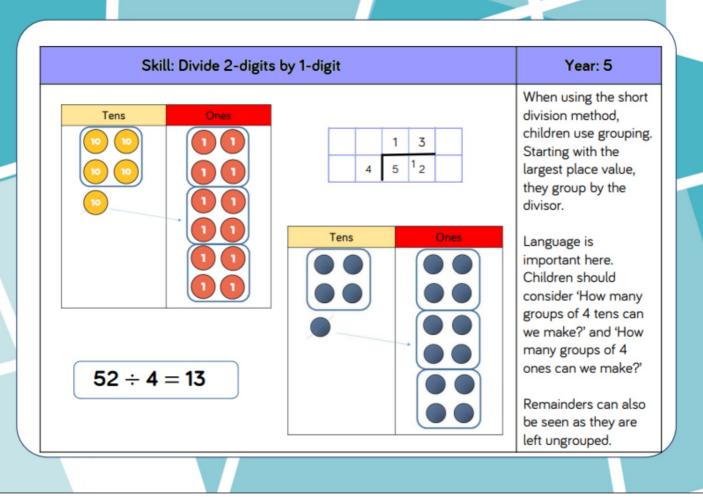


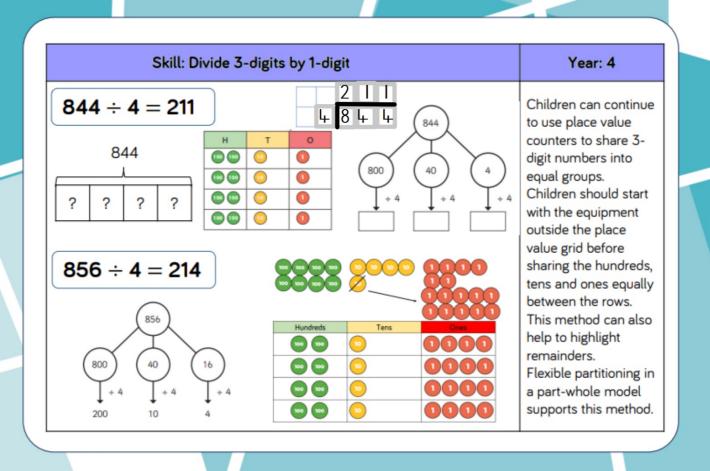


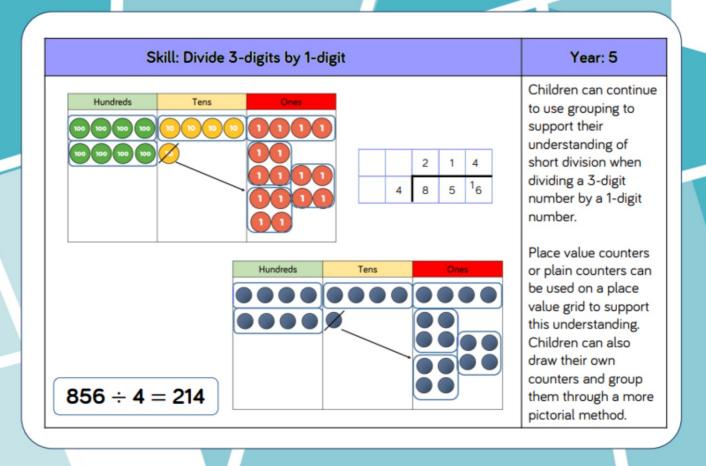


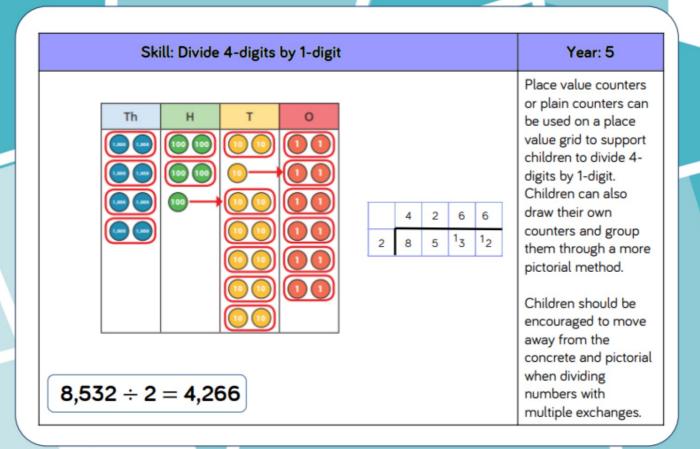


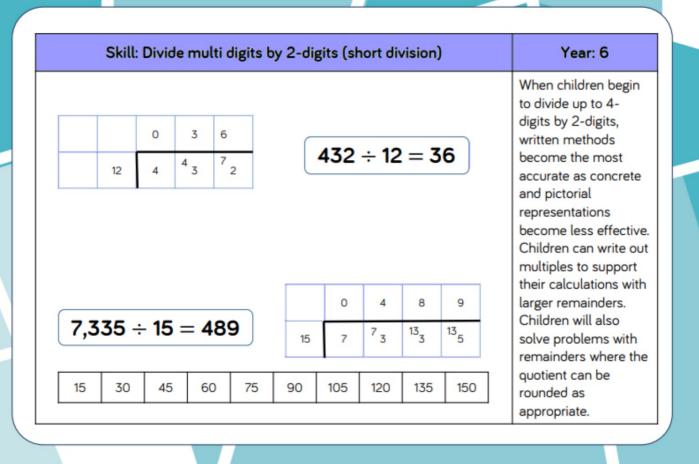












Written long division:

| Skill: Divide multi di | Year: 6 | | | |
|--|---|---|--|--|
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 10 20 30 40 50 60 70 80 90 100 | 5 10 15 20 25 30 35 40 45 50 | 15 30 45 60 75 90 105 120 135 150 | When a remainder is left at the end of a calculation, children can either leave it as a remainder or convert it to a fraction. This will depend on the context of the question. Children can also answer questions where the quotient needs to be rounded according to the context. |

NB - Use TJ eg if dividing by 19 then use multiples of 20 to help.

Written long division:

| Skill: Divide multi dig | Year: 6 | | | |
|--|--------------------------------|---------------------------|--------------------------------|---|
| 2278 ÷ 67 = 34 0 0 3 4 6 7 2 2 7 8 - 2 0 1 1 0 2 6 8 - 2 6 8 0 | 60 120 180 240 300 | 7 4 21 28 35 | 67 134 201 268 335 | In the End of Key Stage SATs Paper I (Arithmetic) the long division questions do not (to date) have remainders. |

 $\ensuremath{\mathsf{NB}}$ – Use TJ eg if dividing by 19 then use multiples of 20 to help.

Glossary

Array – An ordered collection of counters, cubes or other item in rows and columns.

Commutative – Numbers can be multiplied in any order.

Dividend – In division, the number that is divided.

Divisor – In division, the number by which another is divided.

Exchange – Change a number or expression for another of an equal value.

Factor – A number that multiplies with another to make a product.

Multiplicand – In multiplication, a number to be multiplied by another.

Partitioning – Splitting a number into its component parts.

Product - The result of multiplying one number by another.

Quotient - The result of a division

Remainder – The amount left over after a division when the divisor is not a factor of the dividend.

Scaling - Enlarging or reducing a number by a given amount, called the scale factor